

## Institute of Physics

## ELECTRIC CIRCUITS

## CURRENT AND CIRCUITS

Charge (Q) coulomb (C)
Current (I) ampere (A)
Potential difference ( $\mathbf{V}$ ) volt ( $\mathbf{V}$ ) 1 volt is the $\mathbf{P D}$ between two points when 1 joule is lost
or gained by each coulomb moving between those points
Energy dissipated per second = IV
1 ohm is one volt per amp $\boldsymbol{R}=\boldsymbol{V} / \boldsymbol{I}$ *

$$
\begin{aligned}
& R_{\text {Total }}=R_{\mathbf{1}}+R_{\mathbf{2}} \\
& \mathbf{1} / \boldsymbol{R}_{\text {Total }}=\mathbf{1} / \boldsymbol{R}_{\mathbf{1}}+\mathbf{1} / \boldsymbol{R}_{\mathbf{2}}
\end{aligned}
$$

1 coulomb is the basic unit of charge
1 ampere is a current of 1 coulomb per second *

Power ( $\boldsymbol{P}$ ) watt ( $\mathbf{W}$ )
Resistance ( $\boldsymbol{R}$ ) ohm ( $\Omega$ )
In series:
In parallel:

## Cells and EMF

The EMF $(\mathcal{E})=$ the energy supplied to each coulomb by the cell Some energy transferred in external resistance $\boldsymbol{R}$ and some in internal resistance $r$
Energy loss per coulomb through $\mathbf{R}$ is $\boldsymbol{V}=\boldsymbol{I} \boldsymbol{R}$
Energy loss per coulomb through cell $\mathbf{r}$ is $\boldsymbol{v}=\boldsymbol{I r}$
So $\mathcal{E}=\boldsymbol{I R}+\boldsymbol{I r}$
$\mathbf{P D}$ across cell $\boldsymbol{V}=\boldsymbol{\mathcal { E }}-\boldsymbol{v}$

## CAPACITORS


$\boldsymbol{Q}$ is the charge displaced from one plate to the other via the circuit
Capacitance ( $\boldsymbol{C}$ ) Farad ( $\mathbf{F}$ ): number of coulombs displaced per volt
$\boldsymbol{C}=\boldsymbol{Q} / \boldsymbol{V}=\varepsilon_{0} \boldsymbol{A} / \boldsymbol{d}(\boldsymbol{A}=$ Area of each plate $\boldsymbol{d}=$ plate separation) (in a vacuum)
Energy stored $=1 / 2 \boldsymbol{Q V}=1 / 2 \boldsymbol{C} \boldsymbol{V}^{2}=\frac{1 /{ }_{2} \boldsymbol{Q}^{2}}{\boldsymbol{C}}$ (Compare with a elastic materials)
In series: $\mathbf{1} / \boldsymbol{C}_{\text {Total }}=\mathbf{1} / \boldsymbol{C}_{\mathbf{1}}+\mathbf{1} / \boldsymbol{C}_{\mathbf{2}}$ in parallel: $\boldsymbol{C}_{\text {Total }}=\boldsymbol{C}_{\mathbf{1}}+\boldsymbol{C}_{\mathbf{2}}$

## Capacitor Discharge

(Compare with Radioactive Decay)
PD across $\boldsymbol{R}: \boldsymbol{V}=\boldsymbol{Q} / \boldsymbol{C}$, and $\boldsymbol{I}=\boldsymbol{V} / \boldsymbol{R}$
Thus $\boldsymbol{I}=\boldsymbol{Q} / \boldsymbol{R} \boldsymbol{C}$ so $\boldsymbol{I}$ is proportional to $\boldsymbol{Q}$
So rate of loss of $\boldsymbol{Q}$ (i.e. $\boldsymbol{I}$ ) is proportional to $\boldsymbol{Q}$ Therefore $\boldsymbol{Q}_{\boldsymbol{t}}=\boldsymbol{Q}_{0} \mathbf{e}^{\left(\frac{-t}{R C}\right)}$
$\boldsymbol{R C}$ is the time constant
$=$ time for $\boldsymbol{Q}$ to fall to $1 / \mathbf{e}$ of original value
"Full" discharge in about 5RC seconds


## FIELDS

FIELDS DUE TO AN ISOLATED SPHERICAL CHARGE OR MASS
Inverse Square Law of Force Due to an isolated charge ( $\boldsymbol{Q}$ ) or mass ( $\boldsymbol{M}$ )


Field Strength $(\boldsymbol{E})$ Vector Force per unit charge (or unit mass) $\boldsymbol{E}, \boldsymbol{g}$
(In general $\varepsilon_{0}$ is multiplied by $\varepsilon_{r}$ the relative permittivity)
Field Strength $=$ Negative Potential gradient $=\mathbf{-} \mathbf{d V} / \mathbf{d r}$ (always)
Field Potential ( $\boldsymbol{V}$ ) Scalar Potential energy of unit electric charge (or unit mass)
Energy required to bring unit electric charge (or mass) from infinity to the point in question.
Electrical: (repulsive force for positive $\boldsymbol{Q}$ so energy supplied) $\boldsymbol{V}_{\text {elec }}=\boldsymbol{k} \boldsymbol{Q} / \mathbf{r}$
Gravitation: (attractive force for positive $\boldsymbol{M}$ so potential well) $\boldsymbol{V}_{\text {grav }}=-\boldsymbol{G} \boldsymbol{M} / \mathbf{r}$
Potential Energy of charge $\boldsymbol{q}$ (mass $\boldsymbol{m}$ ) in the field: $\boldsymbol{q} \boldsymbol{V}_{\text {elec }} ; \boldsymbol{m} \boldsymbol{V}_{\text {grav }}$

## PARALLEL FIELDS

Field Strength is uniform and the negative of the potential gradient $\boldsymbol{E}=-\boldsymbol{V} / \boldsymbol{d}$

## MAGNETIC FIELDS

Magnetic Field Strength ( $\boldsymbol{B}$ ) tesla ( $\mathbf{T}$ ) Vector 1 tesla is the magnetic field strength that gives rise to a force of 1 N per metre of a wire carrying 1 amp .
Density of field lines in diagrams is proportional to field strength.

## Forces in a magnetic field

1) on a wire length $\ell$ carrying current $I$ (assume all are perpendicular). $\boldsymbol{F}=\boldsymbol{B} \boldsymbol{I} \ell$
2) on a charge $\boldsymbol{q}$ travelling with speed $\boldsymbol{v}$ perpendicular to magnetic field: $\boldsymbol{F}=\boldsymbol{B q} \boldsymbol{V}$ Charge moves in arc of circle of radius $\boldsymbol{r}=\boldsymbol{m v} \boldsymbol{q} \boldsymbol{q} \boldsymbol{B}$ Magnetic Flux ( $\phi$ ) weber (Wb)


Through an area $\boldsymbol{A}: \phi=\boldsymbol{B A}$ (field lines perpendicular to $\boldsymbol{A}$ ).

## Induced EMF in a magnetic field

For a coil with $\boldsymbol{N}$ turns, each with flux $\phi, \varepsilon=-\boldsymbol{N} \mathbf{d} \phi / \mathbf{d} t$

## WAVES

## ENERGY TRANSFER BY WAVES

Transfer of energy without the transfer of matter
Transverse and Longitudinal $\boldsymbol{v}=\boldsymbol{f} \lambda: \boldsymbol{v}=$ velocity: $\boldsymbol{f}=$ frequency: $\lambda=$ wavelength

## INTERFERENCE

## Two-source

Assume that waves at $\mathbf{S}_{\mathbf{1}}$ and $\mathbf{S}_{\mathbf{2}}$ are a) Coherent
b) In phase

If Path Difference $=\boldsymbol{n} \lambda$ then in phase at $\mathbf{A}$ and $\mathbf{B}$ so Constructive Interference at $\mathbf{A}$ and $\mathbf{B}$ $\boldsymbol{\operatorname { s i n }} \theta=\boldsymbol{n} \lambda / \boldsymbol{d} \quad \lambda / \boldsymbol{d}=\boldsymbol{s} / \mathbf{L}$


## Diffraction grating (multiple source)

Different wavelengths produce constructive interference at different angles $\boldsymbol{n} \lambda=\boldsymbol{d} \boldsymbol{\operatorname { s i n }} \theta$ Same formula as two source, but narrow distinct lines, d usually small so $\theta$ large.


## DIFFRACTION

## Diffraction Pattern from Single Slit

Diffraction (i.e. spreading) results from interruption of part of the wave front. Radiation wavelength $\lambda$. Slit width $\boldsymbol{b}$. Electrons and other particles can be diffracted to show their wave properties.

## ELECTROMAGNETIC RADIATION Speed

Interaction of electric and magnetic fields limits the speed of light in a vacuum to: $\boldsymbol{c}=\frac{\mathbf{1}}{\sqrt{\varepsilon_{0} \mu_{o}}}$

Single Slit


Intensity

## Energy of a photon

$\boldsymbol{E}=\boldsymbol{h} \boldsymbol{f}$ ( $\boldsymbol{h}$ is the Planck constant)

## RADIOACTIVITY

## NUCLEAR STRUCTURE

Atomic (proton) number $\boldsymbol{Z}=$ number of protons (and electrons) in the atom (determines the chemical properties)
Mass (nucleon) number $\boldsymbol{A}=$ number of protons plus number of neutrons The strong nuclear force holds together all the nucleons.
(Number of neutrons $(\boldsymbol{n})$ approximately the same as the number of protons $(\boldsymbol{p})$ ).

## Isotopes

Atoms with same atomic number (and so chemically similar) but different atomic mass number

## NUCLEAR DECAY

## Alpha emission

(Helium nucleus: ${ }_{2}^{4} \mathbf{H e}, 2 p+2 n$ )
Beta minus emission
High-energy electron (and antineutrino): emission by "weak interaction"

## Gamma emission


neutron 'loses' electron and converts to proton

Electromagnetic radiation (high frequency)

## Decay Constant

$\lambda=$ probability of decay in a fixed time

$=-(\mathbf{d} / / \mathbf{d} t) / N$
When some have decayed fewer remain so the rate of decay falls.
$\boldsymbol{N}_{\boldsymbol{t}}=\boldsymbol{N}_{o} \mathbf{e}^{-\lambda \boldsymbol{t}}$ (cf. decay of charge on a capacitor)

## Half-life ( $\boldsymbol{T}_{1 / 2}$ )

Time for half to decay $\boldsymbol{T}_{1 / 2}=\ln 2 / \lambda=0.69 / \lambda$

## Radiation Quantities and Units

Activity becquerel $(\mathbf{B q})$ is one disintegration per second
Absorbed dose gray ( $\mathbf{G y}$ ) is the dose when 1 joule is absorbed by 1 kg of tissue Dose equivalent sievert ( $\mathbf{S v}$ ) is related to the biological harm caused by the absorbed dose. *

## Binding energy

If nucleus is bound its mass will be less ( $\Delta \boldsymbol{m}$ ) than the sum of its parts.
Binding energy $=\Delta \boldsymbol{m} \boldsymbol{c}^{2}$

## MISCELLANEOUS

## IDEAL GASES

Pressure $(\boldsymbol{P})$ pascal $(\mathbf{P a}): 1 \mathbf{1 P a}=1$ newton per square metre
$\boldsymbol{P}={ }^{1} / 3 \rho \overline{\boldsymbol{c}^{2}}$ For 1 mole $\boldsymbol{P} \boldsymbol{V}_{m}=\boldsymbol{R} \boldsymbol{T}$

## THERMAL EFFECTS

$\Delta \boldsymbol{Q}=\boldsymbol{m} \boldsymbol{c} \Delta \theta$ Particles have energy of the order $\boldsymbol{k} \boldsymbol{T} . \quad \boldsymbol{T}$ (kelvin) $=\theta^{\circ} \mathrm{C}+\mathbf{2 7 3 . 1 5}$
Boltzmann factor $\boldsymbol{n}_{1} / \boldsymbol{n}_{\mathbf{2}}=\mathbf{e}^{\left(\frac{-\boldsymbol{E}}{\boldsymbol{k} \boldsymbol{T}}\right)}$

## ELASTIC MATERIALS

Stress $\sigma=\boldsymbol{F} / \mathbf{A}(\mathbf{P a})$ Strain $\varepsilon=\boldsymbol{x} / \boldsymbol{L}$ (no unit) The Young Modulus $(\boldsymbol{E})=\sigma / \varepsilon(\mathbf{P a})$


Elastic Strain Energy $=1 / 2 \boldsymbol{k} \mathbf{x}^{\mathbf{2}}$ (Compare with capacitors)

## ATOMIC ENERGY AND LINE SPECTRA

Electrons in atoms regarded as matter waves
De Broglie wavelength for electrons $\lambda=\mathbf{h} / \mathbf{m v}$ Series of "allowed" energy levels and consequent characteristic spectrum

## PHOTOELECTRIC EFFECT

Photons incident on a surface may cause electrons to be emitted. Energy of electron is determined by frequency of incident radiation and surface material

$W=$ work function (for material involved)

## SIMPLE HARMONIC MOTION

Occurs when the force on an object is directed towards a point and its magnitude is proportional to the distance from a point. $\boldsymbol{F}=-\mathbf{k x}$


Acceleration $=-\omega^{2} \mathbf{x}=-\left(\begin{array}{lll}(k / m) & \mathbf{x} & \boldsymbol{T}={ }^{2 \pi} / \omega \quad \boldsymbol{T}=\mathbf{2 \pi}(\mathrm{m} / \mathrm{k})^{1 / 2}\end{array}\right.$
Maximum velocity $=\omega \boldsymbol{A}(\boldsymbol{A}=$ amplitude $)$. Displacement $=\boldsymbol{A} \cos (\omega \boldsymbol{t}+\phi)$
Energy of oscillation $=1 / 2 \boldsymbol{k} \boldsymbol{A}^{2}=1 / 2 m \boldsymbol{v}^{2}+1 / 2 \boldsymbol{k x}^{2}$

## MECHANICS

## MECHANICAL QUANTITIES

Mass (m) kilogram (kg) Scalar
The mass of an object is a measure of the difficulty of changing its velocity. *
$\mathbf{1 k g}$ is the mass of the international prototype of the kilogram stored in Paris.

## Force ( $\boldsymbol{F}$ ) newton ( $\mathbf{N}$ ) Vector

An unbalanced force causes a mass to accelerate: $\boldsymbol{F}=\boldsymbol{m a}$
1 newton is the force required to accelerate $\mathbf{1} \mathbf{~ k g}$ at $\mathbf{1} \mathbf{~ m ~ s}^{-2}$
Weight of an object: is the gravitational force between it and the Earth
On the Earth's surface $\mathbf{1 k g}$ weighs approximately $\mathbf{1 0} \mathbf{N}$

## Energy (E) joule (J) Scalar

1 joule is the energy change when a force of 1 newton acts through 1 metre gravitational potential energy change $=$ weight x vertical distance moved $=\boldsymbol{m g} \boldsymbol{h}$ Kinetic energy $=\mathbf{1} \boldsymbol{2} \boldsymbol{m} \boldsymbol{v}^{\mathbf{2}}$

Power ( $\boldsymbol{P}$ ) watt (W) Scalar
Rate of transforming energy 1 watt $=\mathbf{1} \mathbf{J s}^{-1}$
Momentum ( $\boldsymbol{p}$ ) mass x velocity. ( $\mathbf{k g} \mathrm{ms}^{-1}$ ) or $\mathbf{N s}$ Vector
Force $=$ rate of change of momentum: Force $x$ time (impulse) = momentum change
Equations of Motion $\boldsymbol{v}=\boldsymbol{u}+\boldsymbol{a t} \quad \boldsymbol{v}^{2}-\boldsymbol{u}^{2}=2 \mathrm{as} \quad \boldsymbol{s}=\boldsymbol{u t}+{ }^{1} \mathbf{I}_{2} \boldsymbol{a} \boldsymbol{t}^{2}$

## CONSERVATION LAWS

Always apply providing the entire system is taken into account.
Energy is conserved, but can transform from one form to another.
Momentum is conserved

## CIRCULAR MOTION

Assume speed is constant (but velocity changing)
$\omega=$ angular velocity ( $\mathbf{v} / \mathbf{r}$ ) (radian/second)
$\boldsymbol{T}=$ period for 1 rotation $\boldsymbol{T}=\mathbf{2} \pi / \omega$


Acceleration (toward centre) $={ }^{v^{2}}{ }_{\boldsymbol{r}}=\omega^{2} \boldsymbol{r}$

## Prefixes

$10^{-24}$
$10^{-21}$
$10^{-18}$
$10^{-15}$
$10^{-12}$
$10^{-9}$
$10^{-6}$
$10^{-3}$
yocto
zepto
atto
femto
pico
nano
$\mu$ (micro)
milli

## DATA

Acceleration of free fall (in UK) $g$
Gravitational field strength (in UK) $g$
Gravitational constant $G$
Electric force constant $k=1 / 4 \pi \varepsilon_{o}$
Speed of light in a vacuum $c$
Permeability of free space $\mu_{o}$
Permittivity of free space $\varepsilon_{o}$
Planck constant $h$
Elementary electron charge $e$
Electron rest mass $m_{e}$
Electronvolt eV
Unified atomic mass constant $u$
Proton rest mass $m_{p}$
Neutron rest mass $m_{n}$
Molar gas constant $R$
Boltzmann constant $k$
Avogadro constant $N_{A}$
Standard Temperature \& Pressure (STP) is Molar volume at STP $V_{m}$
$=9.81 \mathrm{~m} \mathrm{~s}^{-2}$
$=9.81 \mathrm{Nkg}^{-1}$
$=6.67 \times 10^{-11} \mathrm{Nm}^{2} \mathrm{~kg}^{-2}$
$=8.98 \times 10^{9} \mathrm{Nm}^{2} \mathrm{C}^{-2}$
$=3.00 \times 10^{8} \mathrm{~ms}^{-1}$
$=4 \pi \times 10^{-7} \mathrm{NA}^{-2}$
$=8.85 \times 10^{-12} \mathrm{Fm}^{-1}$
$=6.63 \times 10^{-34} \mathrm{~J} \mathrm{~S}$
$=-1.60 \times 10^{-19} \mathrm{C}$
$=9.11 \times 10^{-31} \mathrm{~kg}$
$=1.60 \times 10^{-19} \mathrm{~J}$
$=1.66 \times 10^{-27} \mathrm{~kg}$
$=1.673 \times 10^{-27} \mathrm{~kg}$
$=1.675 \times 10^{-27} \mathrm{~kg}$
$=8.31 \mathrm{J}. \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$
$=1.38 \times 10^{-23} \mathrm{JK}^{-1}$
$=6.02 \times 10^{23} \mathrm{~mol}^{-1}$
273.15 K and $1.01 \times 10^{5} \mathrm{~Pa}$
$=22.4 \times 10^{-3} \mathrm{~m}^{3} \mathrm{~mol}^{-1}$

## Helpful Websites

www.bubl.ac.uk/link • A general source www.psigate.ac.uk • Search information portal www.eevl.ac.uk • Engineering (and some science) data www.npl.co.uk/thelearningroom • National Physical Laboratory http://education.iop.org • Institute of Physics site www.physics.org • IOP site for homework help

## Author's Note

This is intended as a quick revision guide and not a definitive reference. While some of the equations are 'correct', they are not a true definition. Where this occurs this is indicated with an asterix (*). Bold is for emphasis and does not signify a vector.
$10^{3}$
$10^{6}$
$10^{9}$
$10^{12}$
$10^{15}$
$10^{18}$
$10^{21}$
$10^{24}$
kilo
Mega
Giga
Tera
Peta
Exa
Zetta
Yotta

